# Motion Field Estimation using MRF

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## Agenda

- What is Edge Flow?
- MRF
- Belief Propagation
- Edge Flow using MRF and Belief Propagation
- Tools Used for Edge Flow
- Results on Synthetic Images
- Results on Natural Images

# Edge Flow

• Motion of Image edges is called Edge Flow



### Markov Random Field



Hidden node variables eg. dispairty values





#### Markov Random Field

$$P(x_{1}, x_{2}, \dots, x_{N}) = \frac{1}{Z} f(x_{1}, x_{2}) g(x_{2}) h(x_{2}, x_{3}, x_{4})$$
 Probability domain  

$$P(x_{1}, x_{2}, \dots, x_{N}) = \frac{1}{Z} e^{F(x_{1}, x_{2}) + G(x_{2}) + H(x_{2}, x_{3}, x_{4})}$$
 Energy (log prob.)  
domain

$$energy(Y, X) = \sum_{i} DataCost(y_i, x_i) + \sum_{j=neighbours of i} SmoothnessCost(x_i, x_j)$$

## **Belief Propagation**





# Edge Flow Using MRF & BP

- Data Cost
  - Sum of Squared Differences
- Smoothness Term
  - Dot Product of Velocity Vectors

### Tools Used

- OpenCV 3.2, 64 Bit
- Matlab 2016b
- Yaml To Read openCV yml in Matlab









### Results on Natural Images

• Stereo Image



#### Results on Natural Image



#### Results of Natural Image









#### Results of Image with Reflections







## References

- A Computational Approach for Obstruction-Free Photography SIGGRAPH 2015, *Michael Rubinstein, Ce Liu, William T. Freeman, Tianfan Xue*
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- LOOPY BELIEF PROPAGATION, MARKOV RANDOM FIELD, STEREO VISION (<u>http://nghiaho.com/?page\_id=1366#LBP</u>)
- MRF Minimization (<u>http://vision.middlebury.edu/MRF/</u>)
- Image-Based Rendering in the Gradient Domain, Johannes Kopf
- Christopher Bishop MLSS 2013 (<u>https://www.youtube.com/watch?v=c0AWH5UFyOk&t=2931s</u>)